

## Advanced Financial Management

## Tuesday 2 June 2015



## Time allowed

Reading and planning: 15 minutes
Writing:
3 hours
This paper is divided into two sections:
Section A - This ONE question is compulsory and MUST be attempted
Section B - TWO questions ONLY to be attempted
Formulae and tables are on pages 9-13.
Do NOT open this paper until instructed by the supervisor.
During reading and planning time only the question paper may
be annotated. You must NOT write in your answer booklet until
instructed by the supervisor.
This question paper must not be removed from the examination hall.


## Section A - This ONE question is compulsory and MUST be attempted

## 1 Yilandwe

Yilandwe, whose currency is the Yilandwe Rand (YR), has faced extremely difficult economic challenges in the past 25 years because of some questionable economic policies and political decisions made by its previous governments. Although Yilandwe's population is generally poor, its people are nevertheless well-educated and ambitious. Just over three years ago, a new government took office and since then it has imposed a number of strict monetary and fiscal controls, including an annual corporation tax rate of $40 \%$, in an attempt to bring Yilandwe out of its difficulties. As a result, the annual rate of inflation has fallen rapidly from a high of $65 \%$ to its current level of $33 \%$. These strict monetary and fiscal controls have made Yilandwe's government popular in the larger cities and towns, but less popular in the rural areas which seem to have suffered disproportionately from the strict monetary and fiscal controls.

It is expected that Yilandwe's annual inflation rate will continue to fall in the coming few years as follows:

| Year | Inflation rate |
| :--- | :---: |
| 1 | $22 \cdot 0 \%$ |
| 2 | $14 \cdot 7 \%$ |
| 3 onwards | $9 \cdot 8 \%$ |

Yilandwe's government has decided to continue the progress made so far, by encouraging foreign direct investment into the country. Recently, government representatives held trade shows internationally and offered businesses a number of concessions, including:
(i) zero corporation tax payable in the first two years of operation; and
(ii) an opportunity to carry forward tax losses and write them off against future profits made after the first two years.

The government representatives also promised international companies investing in Yilandwe prime locations in towns and cities with good transport links.

## Imoni Co

Imoni Co, a large listed company based in the USA with the US dollar (\$) as its currency, manufactures high tech diagnostic components for machinery, which it exports worldwide. After attending one of the trade shows, Imoni Co is considering setting up an assembly plant in Yilandwe where parts would be sent and assembled into a specific type of component, which is currently being assembled in the USA. Once assembled, the component will be exported directly to companies based in the European Union (EU). These exports will be invoiced in Euro (€).

## Assembly plant in Yilandwe: financial and other data projections

It is initially assumed that the project will last for four years. The four-year project will require investments of YR21,000 million for land and buildings, YR18,000 million for machinery and YR9,600 million for working capital to be made immediately. The working capital will need to be increased annually at the start of each of the next three years by Yilandwe's inflation rate and it is assumed that this will be released at the end of the project's life.

It can be assumed that the assembly plant can be built very quickly and production started almost immediately. This is because the basic facilities and infrastructure are already in place as the plant will be built on the premises and grounds of a school. The school is ideally located, near the main highway and railway lines. As a result, the school will close and the children currently studying there will be relocated to other schools in the city. The government has kindly agreed to provide free buses to take the children to these schools for a period of six months to give parents time to arrange appropriate transport in the future for their children.

The current selling price of each component is $€ 700$ and this price is likely to increase by the average EU rate of inflation from year 1 onwards.

The number of components expected to be sold every year are as follows:

| Year | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Sales component units (000s) | 150 | 480 | 730 | 360 |

The parts needed to assemble into the components in Yilandwe will be sent from the USA by Imoni Co at a cost of $\$ 200$ per component unit, from which Imoni Co would currently earn a pre-tax contribution of $\$ 40$ for each component unit. However, Imoni Co feels that it can negotiate with Yilandwe's government and increase the transfer price to $\$ 280$ per component unit. The variable costs related to assembling the components in Yilandwe are currently

YR15,960 per component unit. The current annual fixed costs of the assembly plant are YR4,600 million. All these costs, wherever incurred, are expected to increase by that country's annual inflation every year from year 1 onwards.

Imoni Co pays corporation tax on profits at an annual rate of $20 \%$ in the USA. The tax in both the USA and Yilandwe is payable in the year that the tax liability arises. A bilateral tax treaty exists between Yilandwe and the USA. Tax allowable depreciation is available at $25 \%$ per year on the machinery on a straight-line basis.

Imoni Co will expect annual royalties from the assembly plant to be made every year. The normal annual royalty fee is currently $\$ 20$ million, but Imoni Co feels that it can negotiate this with Yilandwe's government and increase the royalty fee by $80 \%$. Once agreed, this fee will not be subject to any inflationary increase in the project's four-year period.

If Imoni Co does decide to invest in an assembly plant in Yilandwe, its exports from the USA to the EU will fall and it will incur redundancy costs. As a result, Imoni Co's after-tax cash flows will reduce by the following amounts:

| Year | $\mathbf{1}$ | $\mathbf{2}$ | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Redundancy and lost contribution | 20,000 | 55,697 | 57,368 | 59,089 |

Imoni Co normally uses its cost of capital of $9 \%$ to assess new projects. However, the finance director suggests that Imoni Co should use a project specific discount rate of $12 \%$ instead.

Other financial information
Current spot rates

| Euro per Dollar | €0.714/\$1 |
| :--- | ---: |
| YR per Euro | YR142/€1 |
| YR per Dollar | YR101.4/\$1 |

Forecast future rates based on expected inflation rate differentials

| Year | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| $Y R / \$ 1$ | $120 \cdot 1$ | $133 \cdot 7$ | $142 \cdot 5$ | $151 \cdot 9$ |
| Year | 1 |  |  |  |
| YR/€1 | $165 \cdot 0$ | $180 \cdot 2$ | $190 \cdot 2$ | $200 \cdot 8$ |

## Expected inflation rates

EU expected inflation rate: Next two years 5\%
EU expected inflation rate: Year 3 onwards 4\%
USA expected inflation rate: Year 1 onwards 3\%

## Required:

(a) Discuss the possible benefits and drawbacks to Imoni Co of setting up its own assembly plant in Yilandwe, compared to licensing a company based in Yilandwe to undertake the assembly on its behalf. (5 marks)
(b) Prepare a report which:
(i) Evaluates the financial acceptability of the investment in the assembly plant in Yilandwe; (21 marks)
(ii) Discusses the assumptions made in producing the estimates, and the other risks and issues which Imoni Co should consider before making the final decision;
(17 marks)
(iii) Provides a reasoned recommendation on whether or not Imoni Co should invest in the assembly plant in Yilandwe.
(3 marks)
Professional marks will be awarded in part (b) for the format, structure and presentation of the report.

## Section B - TWO questions ONLY to be attempted

2 The treasury department of Chawan Co, a listed company, aims to maintain a portfolio of around $\$ 360$ million consisting of equity shares, corporate bonds and government bonds, which it can turn into cash quickly for investment projects. Chawan Co is considering disposing 27 million shares, valued at $\$ 2.15$ each, which it has invested in Oden Co. The head of Chawan Co's treasury department is of the opinion that, should the decision be made to dispose of its equity stake in Oden Co, this should be sold through a dark pool network and not sold on the stock exchange where Oden Co's shares are listed. In the last few weeks, there have also been rumours that Oden Co may become subject to a takeover bid.

Oden Co operates in the travel and leisure (T\&L) sector, and the poor weather conditions in recent years, coupled with a continuing recession, has meant that the $T \& L$ sector is under-performing. Over the past three years, sales revenue fell by an average of $8 \%$ per year in the T\&L sector. However, there are signs that the economy is starting to recover, but this is by no means certain.

Given below are extracts from the recent financial statements and other financial information for Oden Co and the T\&L sector.

Oden Co
Year ending 31 May (all amounts in \$m)

|  | 2013 | 2014 | 2015 |
| :---: | :---: | :---: | :---: |
| Total non-current assets | 972 | 990 | 980 |
| Total current assets | 128 | 142 | 126 |
| Total assets | 1,100 | 1,132 | 1,106 |
| Equity |  |  |  |
| Ordinary shares (\$0.50) | 300 | 300 | 300 |
| Reserves | 305 | 329 | 311 |
| Total equity | 605 | 629 | 611 |
| Non-current liabilities |  |  |  |
| Bank loans | 115 | 118 | 100 |
| Bonds | 250 | 250 | 260 |
| Total non-current liabilities | 365 | 368 | 360 |
| Current liabilities |  |  |  |
| Trade and other payables | 42 | 45 | 37 |
| Bank overdraft | 88 | 90 | 98 |
| Total current liabilities | 130 | 135 | 135 |
| Total equity and liabilities | 1,100 | 1,132 | 1,106 |

## Oden Co

Year ending 31 May (all amounts in \$m)

|  | 2013 | 2014 | 2015 |
| :---: | :---: | :---: | :---: |
| Sales revenue | 1,342 | 1,335 | 1,185 |
| Operating profit | 218 | 203 | 123 |
| Finance costs | (23) | (27) | (35) |
| Profit before tax | 195 | 176 | 88 |
| Taxation | (35) | (32) | (16) |
| Profit for the year | 160 | 144 | 72 |

Other financial information (Based on annual figures till 31 May of each year)

|  | 2012 | 2013 | 2014 | 2015 |
| :--- | ---: | ---: | ---: | ---: |
| Oden Co average share price (\$) | $2 \cdot 10$ | $2 \cdot 50$ | $2 \cdot 40$ | $2 \cdot 20$ |
| Oden Co dividend per share (\$) | $0 \cdot 15$ | $0 \cdot 18$ | 0.20 | $0 \cdot 15$ |
| T\&L sector average share price (\$) | $3 \cdot 80$ | $4 \cdot 40$ | $4 \cdot 30$ | $4 \cdot 82$ |
| T\&L sector average earnings per share (\$) | 0.32 | 0.36 | $0 \cdot 33$ | 0.35 |
| T\&L sector average dividend per share (\$) | $0 \cdot 25$ | $0 \cdot 29$ | $0 \cdot 29$ | 0.31 |
| Oden Co's equity beta | 1.5 | 1.5 | 1.6 | 2.0 |
| T\&L sector average equity beta | 1.5 | 1.4 | 1.5 | 1.6 |

The risk-free rate and the market return have remained fairly constant over the last ten years at $4 \%$ and $10 \%$ respectively.

Required:
(a) Explain what a dark pool network is and why Chawan Co may want to dispose of its equity stake in Oden Co through one, instead of through the stock exchange where Oden Co's shares are listed.
(b) Discuss whether or not Chawan Co should dispose of its equity stake in Oden Co. Provide relevant calculations to support the discussion.

Note: Up to 10 marks are available for the calculations.

3 In order to raise funds for future projects, the management of Bento Co, a large manufacturing company, is considering disposing of one of its subsidiary companies, Okazu Co, which is involved in manufacturing rubber tubing. They are considering undertaking the disposal through a management buy-out (MBO) or a management buy-in (MBI). Bento Co wants $\$ 60$ million from the sale of Okazu Co.

Given below are extracts from the most recent financial statements for Okazu Co:

## Year ending 30 April (all amounts in \$000)

|  | 2015 |
| :---: | :---: |
| Total non-current assets | 40,800 |
| Total current assets | 12,300 |
| Total assets | 53,100 |
| Equity | 24,600 |
| Non-current liabilities | 16,600 |
| Current liabilities |  |
| Trade and other payables | 7,900 |
| Bank overdraft | 4,000 |
| Total current liabilities | 11,900 |
| Total equity and liabilities | 53,100 |

Year ending 30 April (all amounts in \$000)

| Sales revenue | 2015 |
| :--- | ---: |
| Operating profit | 54,900 |
| Finance costs | 12,200 |
| Profit before tax | 1,600 |
| Taxation | 10,600 |
| Profit for the year | 2,120 |
| 8,480 |  |

Notes relating to the financial statements above:
(i) Current assets, non-current assets and the trade and other payables will be transferred to the new company when Okazu Co is sold. The bank overdraft will be repaid by Bento Co prior to the sale of Okazu Co.
(ii) With the exception of the bank overdraft, Bento Co has provided all the financing to Okazu Co. No liabilities, except the trade and other payables specified above, will be transferred to the new company when Okazu Co is sold.
(iii) It is estimated that the market value of the non-current assets is 30\% higher than the book value and the market value of the current assets is equivalent to the book value.
(iv) The group finance costs and taxation are allocated by Bento Co to all its subsidiaries in pre-agreed proportions.

Okazu Co's senior management team has approached Dofu Co, a venture capital company, about the proposed MBO. Dofu Co has agreed to provide leveraged finance for a $50 \%$ equity stake in the new company on the following basis:
(i) $\$ 30$ million loan in the form of an $8 \%$ bond on which interest is payable annually, based on the loan amount outstanding at the start of each year. The bond will be repaid on the basis of fixed equal annual payments (constituting of interest and principal) over the next four years;
(ii) $\$ 20$ million loan in the form of a $6 \%$ convertible bond on which interest is payable annually. Conversion may be undertaken on the basis of 50 equity shares for every $\$ 100$ from the beginning of year five onwards;
(iii) $5,000,000 \$ 1$ equity shares for $\$ 5,000,000$.

Okazu Co's senior management will contribute $\$ 5,000,000$ for $5,000,000 \$ 1$ equity shares and own the remaining $50 \%$ of the equity stake.

As a condition for providing the finance, Dofu Co will impose a restrictive covenant that the new company's gearing ratio will be no higher than $75 \%$ at the end of its first year of operations, and then fall to no higher than $60 \%, 50 \%$ and $40 \%$ at the end of year two to year four respectively. The gearing ratio is determined by the book value of debt divided by the combined book values of debt and equity.

After the MBO, it is expected that earnings before interest and tax will increase by $11 \%$ per year and annual dividends of $25 \%$ on the available earnings will be paid for the next four years. It is expected that the annual growth rate of dividends will reduce by $60 \%$ from year five onwards following the MBO. The new company will pay tax at a rate of $20 \%$ per year. The new company's cost of equity has been estimated at $12 \%$.

## Required:

(a) Distinguish between a management buy-out (MBO) and a management buy-in (MBI). Discuss the relative benefits and drawbacks to Okazu Co if it is disposed through a MBO instead of a MBI.
(b) Estimate, showing all relevant calculations, whether the restrictive covenant imposed by Dofu $\mathrm{Co}_{0}$ is likely to be met.
(c) Discuss, with supporting calculations, whether or not an MBO would be beneficial for Dofu Co and Okazu Co's senior management team.

4 For a number of years Daikon Co has been using forward rate agreements to manage its exposure to interest rate fluctuations. Recently its chief executive officer (CEO) attended a talk on using exchange-traded derivative products to manage risks. She wants to find out by how much the extra cost of the borrowing detailed below can be reduced, when using interest rate futures, options on interest rate futures, and a collar on the options, to manage the interest rate risk. She asks that detailed calculations for each of the three derivative products be provided and a reasoned recommendation to be made.

Daikon Co is expecting to borrow $\$ 34,000,000$ in five months' time. It expects to make a full repayment of the borrowed amount in 11 months' time. Assume it is 1 June 2015 today. Daikon Co can borrow funds at LIBOR plus 70 basis points. LIBOR is currently $3 \cdot 6 \%$, but Daikon Co expects that interest rates may increase by as much as 80 basis points in five months' time.

The following information and quotes from an appropriate exchange are provided on LIBOR-based $\$$ futures and options.

Three-month $\$$ December futures are currently quoted at $95 \cdot 84$. The contract size is $\$ 1,000,000$, the tick size is $0.01 \%$ and the tick value is $\$ 25$.

Options on three-month $\$$ futures, $\$ 1,000,000$ contract, tick size $0.01 \%$ and tick value $\$ 25$. Option premiums are in annual \%.

| December calls | Strike price | December puts |
| :---: | :---: | :---: |
| 0.541 | 95.50 | 0.304 |
| 0.223 | 96.00 | 0.508 |

## Initial assumptions

It can be assumed that settlement for both the futures and options contracts is at the end of the month; that basis diminishes to zero at a constant rate until the contract matures and time intervals can be counted in months; that margin requirements may be ignored; and that if the options are in-the-money, they will exercised at the end of the hedge instead of being sold.

## Further issues

In the talk, the CEO was informed of the following issues:
(i) Futures contracts will be marked-to-market daily. The CEO wondered what the impact of this would be if 50 futures contracts were bought at $95 \cdot 84$ on 1 June and 30 futures contracts were sold at $95 \cdot 61$ on 3 June, based on the \$ December futures contract given above. The closing settlement prices are given below for four days:

Date Settlement price
1 June $\quad 95.84$
2 June $\quad 95 \cdot 76$
3 June $\quad 95.66$
4 June $\quad 95.74$
(ii) Daikon Co will need to deposit funds into a margin account with a broker for each contract they have opened, and this margin will need to be adjusted when the contracts are marked-to-market daily.
(iii) It is unlikely that option contracts will be exercised at the end of the hedge period unless they have reached expiry. Instead, they more likely to be sold and the positions closed.

## Required:

(a) Based on the three hedging choices available to Daikon Co and the initial assumptions given above, draft a response to the chief executive officer's (CEO) request made in the first paragraph of the question.
(15 marks)
(b) Discuss the impact on Daikon Co of each of the three further issues given above. As part of the discussion, include the calculations of the daily impact of the mark-to-market closing prices on the transactions specified by the CEO.

## Formulae

Modigliani and Miller Proposition 2 (with tax)

$$
k_{e}=k_{e}^{i}+(1-T)\left(k_{e}^{i}-k_{d}\right) \frac{V_{d}}{V_{e}}
$$

The Capital Asset Pricing Model

$$
E\left(r_{i}\right)=R_{f}+\beta_{i}\left(E\left(r_{m}\right)-R_{f}\right)
$$

The asset beta formula

$$
\beta_{\mathrm{a}}=\left[\frac{\mathrm{V}_{\mathrm{e}}}{\left(\mathrm{~V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{e}}\right]+\left[\frac{\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})}{\left(\mathrm{V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{d}}\right]
$$

The Growth Model

$$
P_{o}=\frac{D_{0}(1+g)}{\left(r_{e}-g\right)}
$$

Gordon's growth approximation

$$
\mathrm{g}=\mathrm{br}
$$

The weighted average cost of capital

$$
\text { WACC }=\left[\frac{V_{e}}{V_{e}+V_{d}}\right] k_{e}+\left[\frac{V_{d}}{V_{e}+V_{d}}\right] k_{d}(1-T)
$$

The Fisher formula

$$
(1+i)=(1+r)(1+h)
$$

Purchasing power parity and interest rate parity

$$
S_{1}=S_{0} \times \frac{\left(1+h_{c}\right)}{\left(1+h_{b}\right)} \quad F_{0}=S_{0} \times \frac{\left(1+i_{c}\right)}{\left(1+i_{b}\right)}
$$

Modified Internal Rate of Return

$$
\operatorname{MIRR}=\left[\frac{P V_{R}}{P V_{I}}\right]^{\frac{1}{n}}\left(1+r_{e}\right)-1
$$

The Black-Scholes option pricing model

$$
\mathrm{c}=\mathrm{P}_{\mathrm{a}} \mathrm{~N}\left(\mathrm{~d}_{1}\right)-\mathrm{P}_{\mathrm{e}} \mathrm{~N}\left(\mathrm{~d}_{2}\right) \mathrm{e}^{-r t}
$$

Where:
$d_{1}=\frac{\ln \left(P_{a} / P_{e}\right)+\left(r+0.5 s^{2}\right) t}{s \sqrt{t}}$
$d_{2}=d_{1}-s \sqrt{t}$

The Put Call Parity relationship

$$
p=c-P_{a}+P_{e} e^{-r t}
$$

## Present Value Table

Present value of 1 i.e. $(1+r)^{-n}$
$\begin{array}{ll}\text { Where } & r=\text { discount rate } \\ n & =\text { number of periods until payment }\end{array}$

Discount rate (r)
Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| (n) | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

## Annuity Table

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

$$
\begin{array}{ll}
\text { Where } & r=\text { discount rate } \\
& n=\text { number of periods }
\end{array}
$$

## Discount rate (r)

Periods

| ( n ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | 2.941 | $2 \cdot 884$ | 2.829 | $2 \cdot 775$ | $2 \cdot 723$ | 2.673 | $2 \cdot 624$ | 2.577 | $2 \cdot 531$ | $2 \cdot 487$ | 3 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | $3 \cdot 465$ | $3 \cdot 387$ | 3.312 | 3.240 | 3.170 | 4 |
| 5 | 4.853 | $4 \cdot 713$ | 4.580 | 4.452 | $4 \cdot 329$ | $4 \cdot 212$ | 4.100 | 3.993 | 3.890 | 3.791 | 5 |
| 6 | $5 \cdot 795$ | 5.601 | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | 4.917 | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | 4.355 | 6 |
| 7 | $6 \cdot 728$ | 6.472 | 6.230 | 6.002 | $5 \cdot 786$ | $5 \cdot 582$ | 5.389 | $5 \cdot 206$ | 5.033 | $4 \cdot 868$ | 7 |
| 8 | $7 \cdot 652$ | 7.325 | 7.020 | 6.733 | 6.463 | $6 \cdot 210$ | 5.971 | $5 \cdot 747$ | $5 \cdot 535$ | $5 \cdot 335$ | 8 |
| 9 | 8.566 | $8 \cdot 162$ | 7.786 | 7.435 | $7 \cdot 108$ | $6 \cdot 802$ | 6.515 | $6 \cdot 247$ | 5.995 | $5 \cdot 759$ | 9 |
| 10 | $9 \cdot 471$ | 8.983 | 8.530 | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | 6.418 | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 368$ | 9.787 | 9.253 | 8.760 | 8.306 | 7.887 | 7.499 | $7 \cdot 139$ | 6.805 | 6.495 | 11 |
| 12 | 11.255 | $10 \cdot 575$ | 9.954 | $9 \cdot 385$ | 8.863 | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 134$ | $11 \cdot 348$ | $10 \cdot 635$ | 9.986 | 9.394 | 8.853 | 8.358 | 7.904 | 7.487 | $7 \cdot 103$ | 13 |
| 14 | 13.004 | $12 \cdot 106$ | 11.296 | $10 \cdot 563$ | 9.899 | $9 \cdot 295$ | $8 \cdot 745$ | $8 \cdot 244$ | 7.786 | 7.367 | 14 |
| 15 | 13.865 | $12 \cdot 849$ | 11.938 | $11 \cdot 118$ | $10 \cdot 380$ | $9 \cdot 712$ | $9 \cdot 108$ | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | $1 \cdot 605$ | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | 2.444 | 2.402 | $2 \cdot 361$ | $2 \cdot 322$ | 2.283 | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | 2.974 | 2.914 | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | 2.639 | $2 \cdot 589$ | 4 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | $3 \cdot 352$ | 3.274 | $3 \cdot 199$ | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | 4.231 | $4 \cdot 111$ | 3.998 | 3.889 | 3.784 | 3.685 | 3.589 | 3.498 | 3.410 | $3 \cdot 326$ | 6 |
| 7 | $4 \cdot 712$ | 4.564 | 4.423 | $4 \cdot 288$ | $4 \cdot 160$ | 4.039 | $3 \cdot 922$ | 3.812 | 3.706 | 3.605 | 7 |
| 8 | $5 \cdot 146$ | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | $4 \cdot 207$ | 4.078 | 3.954 | 3.837 | 8 |
| 9 | 5.537 | $5 \cdot 328$ | $5 \cdot 132$ | 4.946 | $4 \cdot 772$ | $4 \cdot 607$ | $4 \cdot 451$ | 4.303 | 4.163 | 4.031 | 9 |
| 10 | $5 \cdot 889$ | $5 \cdot 650$ | $5 \cdot 426$ | $5 \cdot 216$ | 5.019 | $4 \cdot 833$ | $4 \cdot 659$ | 4.494 | $4 \cdot 339$ | $4 \cdot 192$ | 10 |
| 11 | $6 \cdot 207$ | 5.938 | 5.687 | $5 \cdot 453$ | $5 \cdot 234$ | 5.029 | $4 \cdot 836$ | 4.656 | $4 \cdot 486$ | 4.327 | 11 |
| 12 | 6.492 | $6 \cdot 194$ | 5.918 | $5 \cdot 660$ | $5 \cdot 421$ | $5 \cdot 197$ | 4.988 | 4.793 | $4 \cdot 611$ | 4.439 | 12 |
| 13 | $6 \cdot 750$ | $6 \cdot 424$ | $6 \cdot 122$ | $5 \cdot 842$ | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | 6.628 | $6 \cdot 302$ | $6 \cdot 002$ | $5 \cdot 724$ | $5 \cdot 468$ | $5 \cdot 229$ | 5.008 | 4.802 | $4 \cdot 611$ | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | 5.847 | 5.575 | $5 \cdot 324$ | 5.092 | $4 \cdot 876$ | $4 \cdot 675$ | 15 |

Standard normal distribution table

|  | $0 \cdot 00$ | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| $0 \cdot 1$ | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| $0 \cdot 2$ | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | $0 \cdot 1026$ | $0 \cdot 1064$ | $0 \cdot 1103$ | $0 \cdot 1141$ |
| $0 \cdot 3$ | $0 \cdot 1179$ | $0 \cdot 1217$ | $0 \cdot 1255$ | $0 \cdot 1293$ | $0 \cdot 1331$ | $0 \cdot 1368$ | $0 \cdot 1406$ | 0.1443 | $0 \cdot 1480$ | $0 \cdot 1517$ |
| $0 \cdot 4$ | $0 \cdot 1554$ | $0 \cdot 1591$ | $0 \cdot 1628$ | $0 \cdot 1664$ | $0 \cdot 1700$ | $0 \cdot 1736$ | $0 \cdot 1772$ | $0 \cdot 1808$ | $0 \cdot 1844$ | $0 \cdot 1879$ |
| 0.5 | 0.1915 | $0 \cdot 1950$ | $0 \cdot 1985$ | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2995 | $0 \cdot 3023$ | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| $0 \cdot 9$ | $0 \cdot 3159$ | 0.3186 | $0 \cdot 3212$ | 0.3238 | $0 \cdot 3264$ | $0 \cdot 3289$ | 0.3315 | 0.3340 | $0 \cdot 3365$ | 0.3389 |
| 1.0 | 0.3413 | 0.3438 | $0 \cdot 3461$ | 0.3485 | $0 \cdot 3508$ | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| $1 \cdot 1$ | 0.3643 | 0.3665 | $0 \cdot 3686$ | 0.3708 | $0 \cdot 3729$ | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| $1 \cdot 2$ | 0.3849 | 0.3869 | $0 \cdot 3888$ | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| $1 \cdot 3$ | 0.4032 | 0.4049 | $0 \cdot 4066$ | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| $2 \cdot 1$ | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| $2 \cdot 2$ | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| $2 \cdot 3$ | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| $2 \cdot 4$ | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| $2 \cdot 6$ | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| $2 \cdot 9$ | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

This table can be used to calculate $N(d)$, the cumulative normal distribution functions needed for the Black-Scholes model of option pricing. If $d_{i}>0$, add 0.5 to the relevant number above. If $d_{i}<0$, subtract the relevant number above from 0.5 .

## End of Question Paper

