## Advanced Financial Management

Thursday 10 June 2010

## Time allowed

Reading and planning: 15 minutes
Writing: 3 hours
This paper is divided into two sections:
Section A - BOTH questions are compulsory and MUST be attempted
Section B - TWO questions ONLY to be attempted
Formulae and tables are on pages 6-10.


Do NOT open this paper until instructed by the supervisor.
During reading and planning time only the question paper may be annotated. You must NOT write in your answer booklet until instructed by the supervisor.

This question paper must not be removed from the examination hall.

## Section A - BOTH questions are compulsory and MUST be attempted

1 The Seal Island Nuclear Power Company has received initial planning consent for an Advanced Boiling Water Reactor. This project is one of a number that has been commissioned by the Government of Roseland to help solve the energy needs of its expanding population of 60 million and meet its treaty obligations by cutting $\mathrm{CO}_{2}$ emissions to $50 \%$ of their 2010 levels by 2030.

The project proposal is now moving to the detailed planning stage which will include a full investment appraisal within the financial plan. The financial plan so far developed has been based upon experience of this reactor design in Japan, the US and South Korea.

The core macro economic assumptions are that Roseland GDP will grow at an annual rate of 4\% (nominal) and inflation will be maintained at the $2 \%$ target set by the Government.

The construction programme is expected to cost $\$ 1$ billion over three years, with construction commencing in January 2012. These capital expenditures have been projected, including expected future cost increases, as follows:

| Year end | 2012 | 2013 | 2014 |
| :--- | :---: | :---: | :---: |
| Construction costs (\$ million) | 300 | 600 | 100 |

Generation of electricity will commence in 2015 and the annual operating surplus in cash terms is expected to be $\$ 100$ million per annum (at 1 January 2015 price and cost levels). This value has been well validated by preliminary studies and includes the cost of fuel reprocessing, ongoing maintenance and systems replacement as well as the continuing operating costs of running the plant. The operating surplus is expected to rise in line with nominal GDP growth. The plant is expected to have an operating life of 30 years.

Decommissioning costs at the end of the project have been estimated at $\$ 600$ million at current (2012) costs. Decommissioning costs are expected to rise in line with nominal GDP growth.

The company's nominal cost of capital is $10 \%$ per annum. All estimates, unless otherwise stated, are at 1 January 2012 price and cost levels.

## Required:

Produce a preliminary briefing note which, on the basis of the above information, includes:
(i) An estimate of the net present value for this project as at the commencement of construction in 2012.
(ii) A discussion of the principal uncertainties associated with this project.
(iii) A sensitivity of the project's net present value (in percentage and in \$), to changes in the construction cost, the annual operating surplus and the decommissioning cost. (Assume that the increase in construction costs would be proportional to the initial investment for each year.)
(iv) An explanation of how simulations, such as the Monte Carlo simulation, could be used to assess the volatility of the net present value of this project.
(4 marks)
Note: the formula for an annuity discounted at an annual rate (i) and where cash flows are growing at an annual rate (g) is as follows:
$A_{n}=\left[\frac{1-\left(\frac{1+g}{1+i}\right)^{n}}{i-g}\right](1+g)$

2 AggroChem Co is undertaking a due diligence investigation of LeverChem Co and is reviewing the potential bid price for an acquisition. You have been appointed as a consultant to advise the company's management on the financial aspects of the bid.

AggroChem is a fully listed company financed wholly by equity. LeverChem is listed on an alternative investment market. Both companies have been trading for over 10 years and have shown strong levels of profitability recently. However, both companies' shares are thinly traded. It is thought that the current market value of LeverChem's shares at $331 / 3 \%$ higher than the book value is accurate, but it is felt that AggroChem shares are not quoted accurately by the market.

The following information is taken from the financial statements of both companies at the start of the current year:

|  | AggroChem \$'000 | LeverChem \$'000 |
| :---: | :---: | :---: |
| Assets less current liabilities | 4,400 | 4,200 |
| Capital Employed |  |  |
| Equity | 4,400 | 1,200 |
| 5-year floating rate loan at yield rate plus 3\% |  | 3,000 |
| Total capital employed | 4,400 | 4,200 |
| Net operating profit after tax (NOPAT) | 580 | 430 |
| Net amount retained for reinvestment in assets | 180 | 150 |

It can be assumed that the retained earnings for both companies are equal to the net reinvestment in assets.
The assets of both companies are stated at fair value. Discussions with the AtReast Bank have led to an agreement that the floating rate loan to LeverChem can be transferred to the combined business on the same terms. The current yield rate is $5 \%$ and the current equity risk premium is $6 \%$. It can be assumed that the risk free rate of return is equivalent to the yield rate. AggroChem's beta has been estimated to be $1 \cdot 26$.

AggroChem Co wants to use the Black-Scholes option pricing (BSOP) model to assess the value of the combined business and the maximum premium payable to LeverChem's shareholders. AggroChem has conducted a review of the volatility of the NOPAT values of both companies since both were formed and has estimated that the volatility of the combined business assets, if the acquisition were to go ahead, would be $35 \%$. The exercise price should be calculated as the present value of a discount (zero-coupon) bond with an identical yield and term to maturity of the current bond.

## Required:

Prepare a report for the management of AggroChem on the valuation of the combined business following acquisition and the maximum premium payable to the shareholders of LeverChem. Your report should:
(i) Using the free cash flow model, estimate the market value of equity for AggroChem Co, explaining any assumptions made.
(9 marks)
(ii) Explain the circumstances in which the Black-Scholes option pricing (BSOP) model could be used to assess the value of a company, including the data required for the variables used in the model.
(5 marks)
(iii) Using the BSOP methodology, estimate the maximum price and premium AggroChem may pay for LeverChem.
(9 marks)
(iv) Discuss the appropriateness of the method used in part (iii) above, by considering whether the BSOP model can provide a meaningful value for a company.

Professional marks will be awarded in question 2 for the clarity and presentation of the report.

## Section B - TWO questions ONLY to be attempted

3 The finance division of GoSlo Motor Corporation has made a number of loans to customers with a current pool value of $\$ 200$ million. The loans have an average term to maturity of four years. The loans generate a steady income to the business of $10.5 \%$ per annum. The company will use $95 \%$ of the loan's pool as collateral for a collateralised loan obligation structured as follows:

- $80 \%$ of the collateral value to support a tranche of A-rated floating rate loan notes offering investors LIBOR plus 140 basis points.
- $10 \%$ of the collateral value to support a tranche of B-rated fixed rate loan notes offering investors $11 \%$.
- $10 \%$ of the collateral value to support a tranche as subordinated certificates (unrated).

In order to minimise interest rate risk, the company has decided to enter into a fixed for variable rate swap on the A-rated floating rate notes exchanging LIBOR for $8 \cdot 5 \%$.

Service charges of $\$ 240$,000 per annum will be charged for administering the income receivable from the loans.
You may ignore prepayment risk.

## Required:

(a) Calculate the expected returns of the investments in each of the three tranches described above. Estimate the sensitivity of the subordinated certificates to a reduction of $1 \%$ in the returns generated by the pool.
(10 marks)
(b) Explain the purpose and the methods of credit enhancement that can be employed on a securitisation such as this scheme.
(c) Discuss the risks inherent to the investors in a scheme such as this.

4 The MandM Company, a large listed company, has two divisions. The first, the MoneyMint division produces coins and notes for the national exchequer and generates $80 \%$ of the company's revenues. The second, the LunarMint division, manufactures a brand of sweets which are very popular with traders in the financial markets. The company is considering disposing of its LunarMint division. The LunarMint business is no longer viewed as part of the core business of the MandM Company. The Chief Executive Officer commented that he could never understand why the company entered into sweet-making in the first place. The LunarMint business is profitable and low risk, but has not been a high priority for investment.

## Required:

Outline the issues that should be considered when disposing of the LunarMint division noting the risks that might be involved.

5 You are the financial manager of Multidrop (Group) a European based company which has subsidiary businesses in North America, Europe, and Singapore. It also has foreign currency balances outstanding with two non-group companies in the UK and Malaysia. Last year the transaction costs of ad-hoc settlements both within the group and with non-group companies were significant and this year you have reached agreement with the non-group companies to enter into a netting agreement to clear indebtedness with the minimum of currency flows. It has been agreed that Multidrop (Europe) will be the principal in the netting arrangement and that all settlements will be made in Euros at the prevailing spot rate.

The summarised list of year end indebtedness is as follows:

| Owed by: | Owed to: |  |
| :--- | :--- | ---: |
| Multidrop (Europe) | Multidrop (US) | US $\$ 6 \cdot 4$ million |
| Multidrop (Singapore) | Multidrop (Europe) | $\mathrm{S} \$ 16$ million |
| Alposong (Malaysia) | Multidrop (US) | $\mathrm{US} \$ 5 \cdot 4$ million |
| Multidrop (US) | Multidrop (Europe) | $€ 8 \cdot 2$ million |
| Multidrop (Singapore) | Multidrop (US) | $\mathrm{US} \$ 5 \cdot 0$ million |
| Multidrop (Singapore) | Alposong (Malaysia) | Rm 25 million |
| Alposong (Malaysia) | NewRing (UK) | $£ 2 \cdot 2$ million |
| NewRing (UK) | Multidrop (Singapore) | $\mathrm{S} \$ 4 \cdot 0$ million |
| Multidrop (Europe) | Alposong (Malaysia) | Rm8.3 million |

Currency cross rates (mid-market) are as follows:

| Currency |  | UK $£$ | US $\$$ | Euro | Sing \$ | Rm |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| 1 UK | $=$ | 1.0000 | 1.4601 | 1.0653 | 2.1956 | 5.3128 |
| 1 US $\$$ | $=$ | 0.6849 | 1.0000 | 0.7296 | 1.5088 | 3.6435 |
| 1 Euro | $=$ | 0.9387 | 1.3706 | 1.0000 | 2.0649 | 4.9901 |
| 1 Sing \$ | $=$ | 0.4555 | 0.6628 | 0.4843 | 1.0000 | 2.4150 |
| 1 Rm | $=$ | 0.1882 | 0.2745 | 0.2004 | 0.4141 | 1.0000 |

You may assume settlement will be at the mid-market rates quoted.

## Required:

(a) Calculate the inter group and inter-company currency transfers that will be required for settlement by Multidrop (Europe).
(b) Discuss the advantages and disadvantages of netting arrangements with both group and non-group companies.

## Formulae

Modigliani and Miller Proposition 2 (with tax)

$$
k_{e}=k_{e}^{i}+(1-T)\left(k_{e}^{i}-k_{d}\right) \frac{V_{d}}{V_{e}}
$$

Two asset portfolio

$$
s_{p}=\sqrt{w_{a}^{2} s_{a}^{2}+w_{b}^{2} s_{b}^{2}+2 w_{a} w_{b} r_{a b} s_{a} s_{b}}
$$

## The Capital Asset Pricing Model

$$
\mathrm{E}\left(\mathrm{r}_{\mathrm{i}}\right)=\mathrm{R}_{\mathrm{f}}+\beta_{\mathrm{i}}\left(\mathrm{E}\left(\mathrm{r}_{\mathrm{m}}\right)-\mathrm{R}_{\mathrm{f}}\right)
$$

The asset beta formula

$$
\beta_{\mathrm{a}}=\left[\frac{\mathrm{V}_{\mathrm{e}}}{\left(\mathrm{~V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{e}}\right]+\left[\frac{\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})}{\left(\mathrm{V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{d}}\right]
$$

## The Growth Model

$$
P_{o}=\frac{D_{0}(1+g)}{\left(r_{e}-g\right)}
$$

## Gordon's growth approximation

$$
\mathrm{g}=\mathrm{br} \mathrm{r}_{\mathrm{e}}
$$

The weighted average cost of capital

$$
\text { WACC }=\left[\frac{V_{e}}{V_{e}+V_{d}}\right] k_{e}+\left[\frac{V_{d}}{V_{e}+V_{d}}\right] k_{d}(1-T)
$$

## The Fisher formula

$$
(1+i)=(1+r)(1+h)
$$

Purchasing power parity and interest rate parity

$$
S_{1}=S_{0} \times \frac{\left(1+\mathrm{h}_{\mathrm{c}}\right)}{\left(1+\mathrm{h}_{\mathrm{b}}\right)} \quad \mathrm{F}_{0}=\mathrm{S}_{0} \times \frac{\left(1+\mathrm{i}_{\mathrm{c}}\right)}{\left(1+\mathrm{i}_{\mathrm{b}}\right)}
$$

The Put Call Parity relationship

$$
p=c-P_{a}+P_{e} e^{-r t}
$$

Modified Internal Rate of Return

$$
M I R R=\left[\frac{P V_{R}}{P V_{I}}\right]^{\frac{1}{n}}\left(1+r_{e}\right)-1
$$

| The Black-Scholes option pricing model | The FOREX modified Black-Scholes option pricing model |
| :---: | :---: |
| $\mathrm{c}=\mathrm{P}_{\mathrm{a}} \mathrm{~N}\left(\mathrm{~d}_{1}\right)-\mathrm{P}_{\mathrm{e}} \mathrm{~N}\left(\mathrm{~d}_{2}\right) \mathrm{e}^{-\mathrm{rt}}$ <br> Where: $\begin{aligned} & d_{1}=\frac{\ln \left(P_{a} / P_{e}\right)+\left(r+0.5 s^{2}\right) t}{s \sqrt{t}} \\ & d_{2}=d_{1}-s \sqrt{t} \end{aligned}$ | $\mathrm{c}=\mathrm{e}^{-\mathrm{rt}}\left[\mathrm{~F}_{0} \mathrm{~N}\left(\mathrm{~d}_{1}\right)-\mathrm{XN}\left(\mathrm{~d}_{2}\right)\right]$ <br> Or $p=e^{-r t}\left[X N\left(-d_{2}\right)-F_{0} N\left(-d_{1}\right)\right]$ <br> Where: $\mathrm{d}_{1}=\frac{\ln \left(F_{0} / X\right)+\mathrm{s}^{2} \mathrm{~T} / 2}{\mathrm{~s} \sqrt{T}}$ <br> and $d_{2}=d_{1}-s \sqrt{T}$ |

Present value of 1 i.e. $(1+r)^{-n}$
Where $r=$ discount rate
$\mathrm{n}=$ number of periods until payment

Discount rate (r)
Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.941 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.305 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| (n) | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

## Annuity Table

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

$$
\begin{array}{ll}
\text { Where } & r=\text { discount rate } \\
& n=\text { number of periods }
\end{array}
$$

Discount rate (r)
Periods

| ( n ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | $2 \cdot 941$ | $2 \cdot 884$ | $2 \cdot 829$ | $2 \cdot 775$ | $2 \cdot 723$ | 2.673 | $2 \cdot 624$ | $2 \cdot 577$ | 2.531 | $2 \cdot 487$ | 3 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | $3 \cdot 387$ | 3.312 | 3.240 | $3 \cdot 170$ | 4 |
| 5 | 4.853 | $4 \cdot 713$ | 4.580 | 4.452 | $4 \cdot 329$ | $4 \cdot 212$ | $4 \cdot 100$ | 3.993 | 3.890 | 3.791 | 5 |
| 6 | $5 \cdot 795$ | $5 \cdot 601$ | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | 4.917 | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | 4.355 | 6 |
| 7 | $6 \cdot 728$ | 6.472 | 6.230 | 6.002 | $5 \cdot 786$ | 5.582 | 5.389 | $5 \cdot 206$ | 5.033 | $4 \cdot 868$ | 7 |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | $6 \cdot 463$ | $6 \cdot 210$ | 5.971 | $5 \cdot 747$ | 5.535 | $5 \cdot 335$ | 8 |
| 9 | 8.566 | $8 \cdot 162$ | 7.786 | 7.435 | 7.108 | $6 \cdot 802$ | 6.515 | 6.247 | 5.995 | $5 \cdot 759$ | 9 |
| 10 | $9 \cdot 471$ | 8.983 | 8.530 | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | $6 \cdot 418$ | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 37$ | 9.787 | 9.253 | $8 \cdot 760$ | 8.306 | 7.887 | 7.499 | $7 \cdot 139$ | $6 \cdot 805$ | $6 \cdot 495$ | 11 |
| 12 | $11 \cdot 26$ | 10.58 | 9.954 | $9 \cdot 385$ | $8 \cdot 863$ | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 13$ | $11 \cdot 35$ | $10 \cdot 63$ | 9.986 | 9.394 | 8.853 | 8.358 | 7.904 | $7 \cdot 487$ | $7 \cdot 103$ | 13 |
| 14 | 13.00 | $12 \cdot 11$ | 11.30 | $10 \cdot 56$ | 9.899 | 9.295 | $8 \cdot 745$ | 8.244 | 7.786 | $7 \cdot 367$ | 14 |
| 15 | 13.87 | $12 \cdot 85$ | 11.94 | $11 \cdot 12$ | $10 \cdot 38$ | $9 \cdot 712$ | 9.108 | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | $0 \cdot 862$ | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | $2 \cdot 444$ | $2 \cdot 402$ | $2 \cdot 361$ | $2 \cdot 322$ | $2 \cdot 283$ | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | $2 \cdot 974$ | $2 \cdot 914$ | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | $2 \cdot 639$ | 2.589 | 4 |
| 5 | $3 \cdot 696$ | 3.605 | $3 \cdot 517$ | 3.433 | $3 \cdot 352$ | $3 \cdot 274$ | $3 \cdot 199$ | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | 4.231 | $4 \cdot 111$ | 3.998 | 3.889 | 3.784 | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 | 6 |
| 7 | $4 \cdot 712$ | 4.564 | 4.423 | 4.288 | $4 \cdot 160$ | 4.039 | 3.922 | 3.812 | 3.706 | $3 \cdot 605$ | 7 |
| 8 | $5 \cdot 146$ | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | 4.207 | 4.078 | 3.954 | 3.837 | 8 |
| 9 | 5.537 | $5 \cdot 328$ | $5 \cdot 132$ | 4.946 | 4.772 | $4 \cdot 607$ | 4.451 | 4.303 | $4 \cdot 163$ | 4.031 | 9 |
| 10 | 5.889 | $5 \cdot 650$ | $5 \cdot 426$ | $5 \cdot 216$ | 5.019 | $4 \cdot 833$ | 4.659 | $4 \cdot 494$ | $4 \cdot 339$ | 4.192 | 10 |
| 11 | $6 \cdot 207$ | 5.938 | $5 \cdot 687$ | $5 \cdot 453$ | $5 \cdot 234$ | 5.029 | 4.836 | $4 \cdot 656$ | $4 \cdot 486$ | 4.327 | 11 |
| 12 | 6.492 | $6 \cdot 194$ | 5.918 | $5 \cdot 660$ | $5 \cdot 421$ | $5 \cdot 197$ | 4.988 | $4 \cdot 793$ | $4 \cdot 611$ | 4.439 | 12 |
| 13 | 6.750 | 6.424 | $6 \cdot 122$ | 5.842 | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | $6 \cdot 628$ | $6 \cdot 302$ | $6 \cdot 002$ | $5 \cdot 724$ | $5 \cdot 468$ | $5 \cdot 229$ | 5.008 | 4.802 | 4.611 | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | $5 \cdot 847$ | 5.575 | $5 \cdot 324$ | 5.092 | $4 \cdot 876$ | $4 \cdot 675$ | 15 |

Standard normal distribution table

|  | $0 \cdot 00$ | $0 \cdot 01$ | $0 \cdot 02$ | $0 \cdot 03$ | $0 \cdot 04$ | $0 \cdot 05$ | $0 \cdot 06$ | $0 \cdot 07$ | $0 \cdot 08$ | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \cdot 0$ | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| $0 \cdot 1$ | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| $0 \cdot 2$ | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | $0 \cdot 1026$ | $0 \cdot 1064$ | $0 \cdot 1103$ | $0 \cdot 1141$ |
| $0 \cdot 3$ | $0 \cdot 1179$ | $0 \cdot 1217$ | $0 \cdot 1255$ | $0 \cdot 1293$ | $0 \cdot 1331$ | $0 \cdot 1368$ | $0 \cdot 1406$ | $0 \cdot 1443$ | $0 \cdot 1480$ | $0 \cdot 1517$ |
| $0 \cdot 4$ | $0 \cdot 1554$ | $0 \cdot 1591$ | $0 \cdot 1628$ | $0 \cdot 1664$ | $0 \cdot 1700$ | $0 \cdot 1736$ | $0 \cdot 1772$ | $0 \cdot 1808$ | $0 \cdot 1844$ | 0.1879 |
| $0 \cdot 5$ | $0 \cdot 1915$ | $0 \cdot 1950$ | $0 \cdot 1985$ | 0.2019 | 0.2054 | $0 \cdot 2088$ | $0 \cdot 2123$ | $0 \cdot 2157$ | 0.2190 | $0 \cdot 2224$ |
| $0 \cdot 6$ | $0 \cdot 2257$ | 0.2291 | 0.2324 | 0.2357 | 0.2389 | $0 \cdot 2422$ | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| $0 \cdot 7$ | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| $0 \cdot 8$ | $0 \cdot 2881$ | 0.2910 | 0.2939 | 0.2967 | 0.2995 | $0 \cdot 3023$ | $0 \cdot 3051$ | $0 \cdot 3078$ | $0 \cdot 3106$ | 0.3133 |
| $0 \cdot 9$ | $0 \cdot 3159$ | 0.3186 | $0 \cdot 3212$ | $0 \cdot 3238$ | $0 \cdot 3264$ | $0 \cdot 3289$ | 0.3315 | $0 \cdot 3340$ | $0 \cdot 3365$ | 0.3389 |
| $1 \cdot 0$ | $0 \cdot 3413$ | 0.3438 | $0 \cdot 3461$ | $0 \cdot 3485$ | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | $0 \cdot 3621$ |
| $1 \cdot 1$ | $0 \cdot 3643$ | $0 \cdot 3665$ | $0 \cdot 3686$ | $0 \cdot 3708$ | 0.3729 | $0 \cdot 3749$ | 0.3770 | $0 \cdot 3790$ | 0.3810 | 0.3830 |
| $1 \cdot 2$ | 0.3849 | 0.3869 | $0 \cdot 3888$ | $0 \cdot 3907$ | 0.3925 | 0.3944 | 0.3962 | $0 \cdot 3980$ | 0.3997 | 0.4015 |
| $1 \cdot 3$ | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| $1 \cdot 4$ | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| $1 \cdot 5$ | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| $1 \cdot 6$ | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| $1 \cdot 8$ | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| $1 \cdot 9$ | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| $2 \cdot 0$ | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| $2 \cdot 1$ | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| $2 \cdot 2$ | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| $2 \cdot 3$ | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| $2 \cdot 4$ | 0.4918 | 0.4920 | $0 \cdot 4922$ | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| $2 \cdot 5$ | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| $2 \cdot 6$ | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| $2 \cdot 7$ | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| $2 \cdot 8$ | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| $2 \cdot 9$ | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| $3 \cdot 0$ | 0.4987 | 0.4987 | 0.4987 | $0 \cdot 4988$ | $0 \cdot 4988$ | $0 \cdot 4989$ | $0 \cdot 4989$ | $0 \cdot 4989$ | $0 \cdot 4990$ | $0 \cdot 4990$ |

## End of Question Paper

