

## Advanced Financial Management

Thursday 4 June 2009



## Time allowed

Reading and planning: 15 minutes
Writing:
3 hours
This paper is divided into two sections:
Section A - BOTH questions are compulsory and MUST be attempted
Section B - TWO questions ONLY to be attempted
Formulae and tables are on pages 9-13.
Do NOT open this paper until instructed by the supervisor.
During reading and planning time only the question paper may
be annotated. You must NOT write in your answer booklet until
instructed by the supervisor.
This question paper must not be removed from the examination hall.

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The question paper begins on page 3.

## Section A - BOTH questions are compulsory and MUST be attempted

1 You have been conducting a detailed review of an investment project proposed by one of the divisions of your business. Your review has two aims: first to correct the proposal for any errors of principle and second, to recommend a financial measure to replace payback as one of the criteria for acceptability when a project is presented to the company's board of directors for approval. The company's current weighted average cost of capital is $10 \%$ per annum.

The initial capital investment is for $\$ 150$ million followed by $\$ 50$ million one year later. The post tax cash flows, for this project, in \$million, including the estimated tax benefit from capital allowances for tax purposes, are as follows:

| Year | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Capital investment (plant and machinery): |  |  |  |  |  |  |  |
| First phase | -127-50 |  |  |  |  |  |  |
| Second phase |  | -36.88 |  |  |  |  |  |
| Project post tax cash flow (\$ millions) |  |  | 44.00 | $68 \cdot 00$ | $60 \cdot 00$ | 35.00 | $20 \cdot 00$ |

Company tax is charged at $30 \%$ and is paid/recovered in the year in which the liability is incurred. The company has sufficient profits elsewhere to recover capital allowances on this project, in full, in the year they are incurred. All the capital investment is eligible for a first year allowance for tax purposes of $50 \%$ followed by a writing down allowance of $25 \%$ per annum on a reducing balance basis.

You notice the following points when conducting your review:

1. An interest charge of $8 \%$ per annum on a proposed $\$ 50$ million loan has been included in the project's post tax cash flow before tax has been calculated.
2. Depreciation for the use of company shared assets of $\$ 4$ million per annum has been charged in calculating the project post tax cash flow.
3. Activity based allocations of company indirect costs of $\$ 8$ million have been included in the project's post tax cash flow. However, additional corporate infrastructure costs of $\$ 4$ million per annum have been ignored which you discover would only be incurred if the project proceeds.
4. It is expected that the capital equipment will be written off and disposed of at the end of year six. The proceeds of the sale of the capital equipment are expected to be $\$ 7$ million which have been included in the forecast of the project's post tax cash flow. You also notice that an estimate for site clearance of $\$ 5$ million has not been included nor any tax saving recognised on the unclaimed writing down allowance on the disposal of the capital equipment.

## Required:

(a) Prepare a corrected project evaluation using the net present value technique supported by a separate assessment of the sensitivity of the project to a $\$ 1$ million change in the initial capital expenditure.
(14 marks)
(b) Estimate the discounted payback period and the duration for this project commenting on the relative advantages and disadvantages of each method.
(5 marks)
(c) Draft a brief report for presentation to the board of directors with a recommendation on the acceptability of this project and on the techniques that the board should consider when reviewing capital investment projects in future.
(8 marks)

Professional marks will be awarded in part (c) for the clarity, presentation and persuasiveness of the report.

2 BBS Stores, a publicly quoted limited company, is considering unbundling a section of its property portfolio. The company believes that it should use the proceeds to reduce the company's medium-term borrowing and to reinvest the balance in the business (option 1). However, the company's investors have argued strongly that a sale and rental scheme would release substantial cash to investors (option 2). You are a financial consultant and have been given the task of assessing the likely impact of these alternative proposals on the company's financial performance, cost of capital and market value.

Attached is the summarised BBS Stores' statement of financial position. The company owns all its stores.

|  | As at year end 2008 \$m | As at year end 2007 \$m |
| :---: | :---: | :---: |
| ASSETS |  |  |
| Non-current assets |  |  |
| Intangible assets | 190 | 160 |
| Property, plant and equipment | 4,050 | 3,600 |
| Other assets | 500 | 530 |
|  | 4,740 | 4,290 |
| Current assets | 840 | 1,160 |
| Total assets | 5,580 | 5,450 |
| LIABILITIES |  |  |
| Current liabilities | 1,600 | 2,020 |
| Non-current liabilities |  |  |
| Medium-term loan notes | 1,130 | 1,130 |
| Other non-financial liabilities | 890 | 900 |
|  | 2,020 | 2,030 |
| Total liabilities | 3,620 | 4,050 |
| Net assets | 1,960 | 1,400 |
| EQUITY |  |  |
| Called up share capital - equity | 425 | 420 |
| Retained earnings | 1,535 | 980 |
| Total equity | 1,960 | 1,400 |

The company's profitability has improved significantly in recent years and earnings for 2008 were $\$ 670$ million (2007: \$540 million).

The company's property, plant and equipment within non-current assets for 2008 are as follows:

|  | Land and <br> buildings <br> $\$ m$ | Fixtures, <br>  <br> equipment <br> $\$ m$ | Assets <br> under <br> construction <br> $\$ m$ | Total <br> $\$ m$ |
| :--- | :---: | :---: | :---: | :---: |
| Year end 2008 <br> At revaluation <br> Accumulated depreciation | 2,297 | $\boxed{2,038}$ | 165 | 6,500 |
| Net book value | $\underline{2,297}$ | $\underline{1,588}$ | $\underline{165}$ | $\underline{(2,450)}$ |

The property portfolio was revalued at the year end 2008. The assets under construction are valued at a market value of $\$ 165$ million and relate to new building.

In recent years commercial property values have risen in real terms by $4 \%$ per annum. Current inflation is $2 \cdot 5 \%$ per annum. Property rentals currently earn an $8 \%$ return.
The proposal is that $50 \%$ of the property portfolio (land and buildings) and $50 \%$ of the assets under construction would be sold to a newly established property holding company called RPH that would issue bonds backed by the assured rental income stream from BBS Stores. BBS Stores would not hold any equity interest in the newly formed company nor would they take any part in its management.

BBS Stores is currently financed by equity in the form of 25 c fully paid ordinary shares with a current market value of 400c per share. The capital debt for the company consists of medium-term loan notes of which $\$ 360$ million are repayable at the end of two years and $\$ 770$ million are repayable at the end of six years. Both issues of mediumterm notes carry a floating rate of LIBOR plus 70 basis points. The interest liability on the six year notes has been swapped at a fixed rate of $5.5 \%$ in exchange for LIBOR which is also currently $5.5 \%$. The reduction in the firm's gearing implied by option 1 would improve the firm's credit rating and reduce its current credit spread by 30 basis points. The change in gearing resulting from the second option is not expected to have any impact upon the firm's credit rating. There has been no alteration in the rating of the company since the earliest debt was issued.

The BBS Stores equity beta is currently 1.824 . A representative portfolio of commercial property companies has an equity beta of 1.25 and an average market gearing (adjusted for tax) of $50 \%$. The risk free rate of return is $5 \%$ and the equity risk premium is $3 \%$. The company's current accounting rate of return on new investment is $13 \%$ before tax. You may assume that debt betas are zero throughout.

The effective rate of company tax is $35 \%$.

## Required:

On the assumption that the property unbundling proceeds, prepare a report for consideration by senior management which should include the following:
(a) A comparative statement showing the impact upon the statement of financial position and on the earnings per share on the assumption that the cash proceeds of the property sale are used:
(i) To repay the debt, repayable in two years, in full and for reinvestment in non-current assets;
(ii) To repay the debt, repayable in two years, in full and to finance a share repurchase at the current share price with the balance of the proceeds.
(13 marks)
(b) An estimate of the weighted average cost of capital for the remaining business under both options on the assumption that the share price remains unchanged.
(10 marks)
(c) An evaluation of the potential impact of each alternative on the market value of the firm (you are not required to calculate a revised market value for the firm).
(6 marks)

Professional marks will be awarded in question 2 for the clarity, presentation and persuasiveness of the report.
(3 marks)
(32 marks)

## Section B - TWO questions ONLY to be attempted

3 You are an importer of stone chippings for building purposes and you have entered into a fixed price contract for the delivery of 10,000 metric tonnes per month for the next six months.

The first delivery is due in one month's time.
Each tonne costs $€ 220$ under the fixed price contract and will be paid in Euros at the end of the month in question. Your domestic currency is the dollar and your supplier is in the Euro area. The current rate of exchange is Euro 0.8333 to the dollar. The quoted forward rates and the risk free interest rates in the dollar zone are as follows:

|  | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Forward Rates (Euros per \$) | 0.8326 | 0.8314 | 0.8302 | 0.8289 | 0.8278 | 0.8267 |
| \$ short zero coupon yield curve | $3.25 \%$ | $3.45 \%$ | $3.50 \%$ | $3.52 \%$ | $3.52 \%$ | $3.52 \%$ |

## Required:

(a) Estimate the forward exchange rate that would be fixed for a six month currency swap with monthly deliveries against the current order of 10,000 metric tonnes per month.
(12 marks)
(b) Outline the advantages and disadvantages of using a plain vanilla currency swap with monthly delivery compared with a strip of forward contracts.

4 You have been appointed as deputy Chief Financial Officer to a large multinational pharmaceutical company with trading interests in 24 countries in sub-Saharan Africa, South America and the Indian sub-continent. Your company also has important trading links with the United States, Malaysia and Singapore. There have been a number of issues arising in the previous six months which have impacted upon the company's business interests.
(i) Following an investigation you discover that commissions were paid to a senior official in one country to ensure that the local drug licensing agency concerned facilitated the acceptance of one of your principal revenue earning drugs for use within its national health service.
(ii) You have discovered that an agent of your firm, aware that the licensing agreement might be forthcoming, purchased several call option contracts on your company's equity.
(iii) A senior member of the firm's treasury team has been taking substantial positions in currency futures in order to protect the risk of loss on the translation of dollar assets into the domestic currency. Over the last 12 months significant profits have been made but the trades do not appear to have been properly authorised. You discover that a long position in $50, \$ 250,000$ contracts is currently held but over the last four weeks the dollar has depreciated by $10 \%$ and all the signs are that it will depreciate considerably more over the next two months.
(iv) One drug company has managed to copy a novel drug that you have just released for the treatment of various forms of skin cancer. You have patent protection in the country concerned but your company has not been able to initiate proceedings through the local courts. Contacts with the trade officials at your embassy in the country concerned suggest that the government has made sure that the proceedings have not been allowed to proceed.
The company's chief financial officer has asked you to look into these issues and, with respect to (iv), any World Trade Organisation (WTO) agreements that might be relevant, and to advise her on how the company should proceed in each case.

## Required:

Prepare a memorandum advising the Chief Financial Officer on the issues involved and recommending how she should, in each case and in the circumstances, proceed.

5 Slow Fashions Ltd is considering the following series of investments for the current financial year 2009:
Project bid proposals (\$000) for immediate investment with the first cash return assumed to follow in 12 months and at annual intervals thereafter.

| Project | Now | 2010 | 2011 | 2012 | 2013 | 2014 | 2015 | NPV | IRR |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| P0801 | -620 | 280 | 400 | 120 |  |  |  | 55 | $16 \%$ |
| P0802 | -640 | 80 | 120 | 200 | 210 | 420 | -30 | 69 | $13 \%$ |
| P0803 | -240 | 120 | 120 | 60 | 10 |  |  | 20 | $15 \%$ |
| P0804 | -1000 | 300 | 500 | 250 | 290 |  |  | 72 | $13 \%$ |
| P0805 | -120 | 25 | 55 | 75 | 21 |  |  | 19 | $17 \%$ |
| P0806 | -400 | 245 | 250 |  |  |  |  | 29 | $15 \%$ |

There is no real option to delay any of these projects. All except project P0801, can be scaled down but not scaled up. P0801 is a potential fixed three-year contract to supply a supermarket chain and cannot be varied. The company has a limited capital budget of $\$ 1.2$ million and is concerned about the best way to allocate its capital to the projects listed. The company has a current cost of finance of $10 \%$ but it would take a year to establish further funding at that rate. Further funding for a short period could be arranged at a higher rate.

## Required:

(a) Draft a capital investment plan with full supporting calculations justifying those projects which should be adopted giving:
(i) The priorities for investment,
(ii) The net present value and internal rate of return of the plan; and
(iii) The net present value per dollar invested on the plan.
(12 marks)
(b) Estimate and advise upon the maximum interest rate which the company should be prepared to pay to finance investment in all of the remaining projects available to it.
(8 marks)
(20 marks)

## Formulae

Modigliani and Miller Proposition 2 (with tax)

$$
k_{e}=k_{e}^{i}+(1-T)\left(k_{e}^{i}-k_{d}\right) \frac{V_{d}}{V_{e}}
$$

Two asset portfolio

$$
s_{p}=\sqrt{w_{a}^{2} s_{a}^{2}+w_{b}^{2} s_{b}^{2}+2 w_{a} w_{b} r_{a b} s_{a} s_{b}}
$$

The Capital Asset Pricing Model

$$
\mathrm{E}\left(\mathrm{r}_{\mathrm{i}}\right)=\mathrm{R}_{\mathrm{f}}+\beta_{\mathrm{i}}\left(\mathrm{E}\left(\mathrm{r}_{\mathrm{m}}\right)-\mathrm{R}_{\mathrm{f}}\right)
$$

The asset beta formula

$$
\beta_{\mathrm{a}}=\left[\frac{\mathrm{V}_{\mathrm{e}}}{\left(\mathrm{~V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{e}}\right]+\left[\frac{\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})}{\left(\mathrm{V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{d}}\right]
$$

## The Growth Model

$$
P_{o}=\frac{D_{0}(1+g)}{\left(r_{e}-g\right)}
$$

## Gordon's growth approximation

$$
\mathrm{g}=\mathrm{br} \mathrm{r}_{\mathrm{e}}
$$

The weighted average cost of capital

$$
\text { WACC }=\left[\frac{V_{e}}{V_{e}+V_{d}}\right] k_{e}+\left[\frac{V_{d}}{V_{e}+V_{d}}\right] k_{d}(1-T)
$$

## The Fisher formula

$$
(1+i)=(1+r)(1+h)
$$

Purchasing power parity and interest rate parity

$$
S_{1}=S_{0} \times \frac{\left(1+h_{c}\right)}{\left(1+h_{b}\right)} \quad F_{0}=S_{0} \times \frac{\left(1+i_{c}\right)}{\left(1+i_{b}\right)}
$$

## The Put Call Parity relationship

$$
\mathrm{p}=\mathrm{c}-\mathrm{P}_{\mathrm{a}}+\mathrm{P}_{\mathrm{e}} \mathrm{e}^{-\mathrm{rt}}
$$

Modified Internal Rate of Return

$$
M I R R=\left[\frac{P V_{R}}{P V_{l}}\right]^{\frac{1}{n}}\left(1+r_{e}\right)-1
$$



## Present Value Table

Present value of 1 i.e. $(1+r)^{-n}$
Where $\quad \begin{aligned} r & =\text { discount rate } \\ n & =\text { number of periods until payment }\end{aligned}$

## Discount rate (r)

Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.941 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.305 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| (n) | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

## Annuity Table

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

$$
\begin{array}{ll}
\text { Where } & r=\text { discount rate } \\
& n=\text { number of periods }
\end{array}
$$

## Discount rate (r)

Periods

| ( n ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | 2.941 | $2 \cdot 884$ | $2 \cdot 829$ | $2 \cdot 775$ | $2 \cdot 723$ | $2 \cdot 673$ | $2 \cdot 624$ | $2 \cdot 577$ | $2 \cdot 531$ | $2 \cdot 487$ | 3 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | $3 \cdot 387$ | 3.312 | 3.240 | $3 \cdot 170$ | 4 |
| 5 | $4 \cdot 853$ | $4 \cdot 713$ | 4.580 | $4 \cdot 452$ | $4 \cdot 329$ | $4 \cdot 212$ | 4.100 | 3.993 | $3 \cdot 890$ | 3.791 | 5 |
| 6 | $5 \cdot 795$ | 5.601 | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | 4.917 | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | 4.355 | 6 |
| 7 | $6 \cdot 728$ | $6 \cdot 472$ | 6.230 | 6.002 | 5.786 | $5 \cdot 582$ | 5.389 | $5 \cdot 206$ | 5.033 | $4 \cdot 868$ | 7 |
| 8 | $7 \cdot 652$ | $7 \cdot 325$ | $7 \cdot 020$ | 6.733 | $6 \cdot 463$ | $6 \cdot 210$ | 5.971 | $5 \cdot 747$ | 5.535 | $5 \cdot 335$ | 8 |
| 9 | 8.566 | 8.162 | $7 \cdot 786$ | 7.435 | 7.108 | 6.802 | 6.515 | 6.247 | 5.995 | $5 \cdot 759$ | 9 |
| 10 | 9.471 | 8.983 | $8 \cdot 530$ | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | $6 \cdot 418$ | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 37$ | $9 \cdot 787$ | $9 \cdot 253$ | 8.760 | 8.306 | 7.887 | 7.499 | $7 \cdot 139$ | $6 \cdot 805$ | $6 \cdot 495$ | 11 |
| 12 | $11 \cdot 26$ | $10 \cdot 58$ | 9.954 | $9 \cdot 385$ | $8 \cdot 863$ | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 13$ | $11 \cdot 35$ | $10 \cdot 63$ | 9.986 | $9 \cdot 394$ | 8.853 | 8.358 | 7.904 | 7.487 | $7 \cdot 103$ | 13 |
| 14 | 13.00 | $12 \cdot 11$ | 11.30 | $10 \cdot 56$ | 9.899 | 9.295 | $8 \cdot 745$ | 8.244 | 7.786 | $7 \cdot 367$ | 14 |
| 15 | $13 \cdot 87$ | $12 \cdot 85$ | 11.94 | $11 \cdot 12$ | $10 \cdot 38$ | $9 \cdot 712$ | $9 \cdot 108$ | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | $0 \cdot 893$ | $0 \cdot 885$ | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | $2 \cdot 444$ | $2 \cdot 402$ | $2 \cdot 361$ | $2 \cdot 322$ | $2 \cdot 283$ | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | $2 \cdot 974$ | 2.914 | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | 2.639 | 2.589 | 4 |
| 5 | $3 \cdot 696$ | 3.605 | $3 \cdot 517$ | 3.433 | 3.352 | 3.274 | 3.199 | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | $4 \cdot 231$ | 4•111 | 3.998 | 3.889 | $3 \cdot 784$ | 3.685 | 3.589 | 3.498 | 3.410 | $3 \cdot 326$ | 6 |
| 7 | $4 \cdot 712$ | $4 \cdot 564$ | $4 \cdot 423$ | 4.288 | $4 \cdot 160$ | 4.039 | 3.922 | 3.812 | 3.706 | $3 \cdot 605$ | 7 |
| 8 | $5 \cdot 146$ | 4.968 | $4 \cdot 799$ | 4.639 | $4 \cdot 487$ | 4.344 | 4.207 | $4 \cdot 078$ | 3.954 | 3.837 | 8 |
| 9 | 5.537 | $5 \cdot 328$ | $5 \cdot 132$ | 4.946 | 4.772 | $4 \cdot 607$ | 4.451 | 4.303 | $4 \cdot 163$ | 4.031 | 9 |
| 10 | 5.889 | $5 \cdot 650$ | $5 \cdot 426$ | 5.216 | 5.019 | $4 \cdot 833$ | $4 \cdot 659$ | 4.494 | $4 \cdot 339$ | 4.192 | 10 |
| 11 | $6 \cdot 207$ | 5.938 | $5 \cdot 687$ | $5 \cdot 453$ | 5.234 | 5.029 | 4.836 | $4 \cdot 656$ | $4 \cdot 486$ | 4.327 | 11 |
| 12 | 6.492 | $6 \cdot 194$ | $5 \cdot 918$ | $5 \cdot 660$ | 5.421 | $5 \cdot 197$ | 4.988 | $4 \cdot 793$ | $4 \cdot 611$ | 4.439 | 12 |
| 13 | 6.750 | $6 \cdot 424$ | $6 \cdot 122$ | 5.842 | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | 6.628 | $6 \cdot 302$ | 6.002 | $5 \cdot 724$ | $5 \cdot 468$ | 5.229 | 5.008 | 4.802 | 4.611 | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | $5 \cdot 847$ | $5 \cdot 575$ | $5 \cdot 324$ | 5.092 | $4 \cdot 876$ | 4.675 | 15 |

Standard normal distribution table

|  | $0 \cdot 00$ | 0.01 | $0 \cdot 02$ | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \cdot 0$ | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| $0 \cdot 1$ | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| $0 \cdot 2$ | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | $0 \cdot 1026$ | $0 \cdot 1064$ | $0 \cdot 1103$ | 0.1141 |
| $0 \cdot 3$ | 0.1179 | $0 \cdot 1217$ | $0 \cdot 1255$ | $0 \cdot 1293$ | $0 \cdot 1331$ | $0 \cdot 1368$ | $0 \cdot 1406$ | 0.1443 | $0 \cdot 1480$ | $0 \cdot 1517$ |
| $0 \cdot 4$ | $0 \cdot 1554$ | $0 \cdot 1591$ | $0 \cdot 1628$ | $0 \cdot 1664$ | $0 \cdot 1700$ | $0 \cdot 1736$ | $0 \cdot 1772$ | $0 \cdot 1808$ | $0 \cdot 1844$ | $0 \cdot 1879$ |
| 0.5 | $0 \cdot 1915$ | $0 \cdot 1950$ | $0 \cdot 1985$ | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| $0 \cdot 6$ | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | $0 \cdot 2881$ | 0.2910 | 0.2939 | 0.2967 | 0.2995 | $0 \cdot 3023$ | 0.3051 | $0 \cdot 3078$ | 0.3106 | 0.3133 |
| 0.9 | $0 \cdot 3159$ | 0.3186 | 0.3212 | 0.3238 | 0.3264 | $0 \cdot 3289$ | 0.3315 | $0 \cdot 3340$ | $0 \cdot 3365$ | 0.3389 |
| 1.0 | $0 \cdot 3413$ | 0.3438 | 0.3461 | $0 \cdot 3485$ | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| $1 \cdot 1$ | $0 \cdot 3643$ | $0 \cdot 3665$ | 0.3686 | $0 \cdot 3708$ | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| $1 \cdot 2$ | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | $0 \cdot 4222$ | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| $2 \cdot 1$ | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| $2 \cdot 2$ | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| $2 \cdot 3$ | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| $2 \cdot 4$ | 0.4918 | $0 \cdot 4920$ | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| $2 \cdot 6$ | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| $2 \cdot 7$ | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| $2 \cdot 8$ | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| $2 \cdot 9$ | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.49987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

This table can be used to calculate $N(d)$, the cumulative normal distribution functions needed for the Black-Scholes model of option pricing. If $d_{i}>0$, add 0.5 to the relevant number above. If $d_{i}<0$, subtract the relevant number above from 0.5 .

## End of Question Paper

