

## Advanced Financial Management

Thursday 10 December 2009

## Time allowed

Reading and planning: 15 minutes
Writing:
3 hours
This paper is divided into two sections:
Section A - BOTH questions are compulsory and MUST be attempted
Section B - TWO questions ONLY to be attempted
Formulae and tables are on pages 9-13.
Do NOT open this paper until instructed by the supervisor.
During reading and planning time only the question paper may
be annotated. You must NOT write in your answer booklet until
instructed by the supervisor.
This question paper must not be removed from the examination hall.

## Section A - BOTH questions are compulsory and MUST be attempted

1 Kodiak Company is a small software design business established four years ago. The company is owned by three directors who have relied upon external accounting services in the past. The company has grown quickly and the directors have appointed you as a financial consultant to advise on the value of the business under their ownership.

The directors have limited liability and the bank loan is secured against the general assets of the business. The directors have no outstanding guarantees on the company's debt.

The company's latest income statement and the extracted balances from the latest statement of financial position are as follows:

| Income Statement | $\$ \mathbf{0 0 0}$ | Financial Position | $\$ 000$ |
| :--- | ---: | :--- | ---: |
| Revenue | 5,000 | Opening non-current assets | 1,200 |
| Cost of Sales | 3,000 | Additions | 66 |
| Gross profit | 2,000 |  | Non-current assets (gross) |
| Other operating costs | 1,877 | Accumulated depreciation | 1,266 |
| Operating profit | 123 | Net book value | 367 |
| Interest on loan | 74 | Net current assets | 899 |
| Profit before tax | 49 | Loan | 270 |
| Income tax expense | 15 | Net Assets Employed | $\underline{(990)}$ |

Profit for the period
During the current year:
(1) Depreciation is charged at $10 \%$ per annum on the year end non-current asset balance before accumulated depreciation, and is included in other operating costs in the income statement.
(2) The investment in net working capital is expected to increase in line with the growth in gross profit.
(3) Other operating costs consisted of:
$\$ 000$
Variable component at $15 \%$ of sales
Fixed costs
Depreciation on non-current assets

750
1,000 127
(4) Revenue and variable costs are projected to grow at $9 \%$ per annum and fixed costs are projected to grow at 6\% per annum.
(5) The company pays interest on its outstanding loan of $7.5 \%$ per annum and incurs tax on its profits at 30\%, payable in the following year. The company does not pay dividends.
(6) The net current assets reported in the statement of financial position contain $\$ 50,000$ of cash.

One of your first tasks is to prepare for the directors a forward cash flow projection for three years and to value the firm on the basis of its expected free cash flow to equity. In discussion with them you note the following:

- The company will not dispose of any of its non-current assets but will increase its investment in new non-current assets by $20 \%$ per annum. The company's depreciation policy matches the currently available tax write off for capital allowances. This straight-line write off policy is not likely to change.
- The directors will not take a dividend for the next three years but will then review the position taking into account the company's sustainable cash flow at that time.
- The level of the loan will be maintained at \$990,000 and, on the basis of the forward yield curve, interest rates are not expected to change.
- The directors have set a target rate of return on their equity of $10 \%$ per annum which they believe fairly represents the opportunity cost of their invested funds.


## Required:

(a) Prepare a three-year cash flow forecast for the business on the basis described above highlighting the free cash flow to equity in each year.
(b) Estimate the value of the business based upon the expected free cash flow to equity and a terminal value based upon a sustainable growth rate of $3 \%$ per annum thereafter.
(c) Advise the directors on the assumptions and the uncertainties within your valuation.
(d) With reference to option pricing theory, advise the directors how limited liability may give a different value to the business from the value estimated in part (b) above.

2 Anchorage Retail Company is a large high street and on-line retailer that has lost its position as the premier quality clothes, household goods and food chain in the European market. Five years previously there had been speculation that the company would be a takeover target for any one of a number of private equity firms. However, a newly appointed and flamboyant Chief Executive Officer, John Bear, initiated a major capital reconstruction and a highly aggressive turnaround strategy.

The reaction to that turnaround strategy was an improvement in the company's share price from $\$ 3$ to $\$ 7$ per share over the subsequent three years. The private equity firms who had been interested in acquiring the company were deterred for two principal reasons. First John Bear had a reputation for his aggressive style and his history of defending his companies against takeover. Second the share price of Anchorage had reached a record high.

In recent months a belief in the investment community had become widespread that the revival of the company's performance had more to do with the reorganisation of the firm's capital than the success of John Bear's turnaround strategy. John Bear insisted, however, that the improvements in the reported 'bottom line' reflected a sustainable improvement in the performance of the business. However, the recent recession in the European retail market following the 'credit crunch' led to a sharp reduction in Anchorage's share price reinforced by concerns in the financial markets that John Bear has become too dominant in the board of the company.

The most recent accounts for Anchorage Retail, in summary form, are as follows:

## Anchorage Retail Company

|  | 2009 $\$ m$ | 2008 $\$ m$ |  | $\begin{gathered} 2009 \\ \$ m \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| Income statement |  |  | Summary cash flow statement |  |
| Sales Turnover | 9,000 | 8,500 |  |  |
| Cost of Sales | 5,500 | 5,250 | Operating cash flow | 1,610 |
| Gross Profit | 3,500 | 3,250 | less interest | (110) |
| less other operating costs | 2,250 | 2,220 | less taxation | (270) |
| Operating profit | 1,250 | 1,030 | Free cash flow before reinvestment | 1,230 |
| Finance Costs | 80 | 110 | Dividend paid | (270) |
| Profit before tax | 1,170 | 920 | CAPEX | (740) |
| Income tax expense (at 30\%) | 310 | 270 | Financing | (70) |
| Profit for the period | 860 | 650 | Net cash flow | 150 |
|  | 2009 | 2008 |  |  |
| Statement of financial position Assets | \$m | \$m |  |  |
| Non-current assets | 4,980 | 4,540 |  |  |
| Current assets | 1,220 | 850 |  |  |
| Total assets | 6,200 | 5,390 |  |  |
| Equity and Liabilities |  |  |  |  |
| Ordinary share capital (25c) | 400 | 425 |  |  |
| Share premium | 230 | 200 |  |  |
| Capital redemption reserve | 2,300 | 2,300 |  |  |
| Other reserves | $(6,540)$ | $(6,500)$ |  |  |
| Retained earnings | 5,990 | 5,400 |  |  |
| Dividends payable | (350) | (270 |  |  |
| Total equity | 2,030 | 1,555 |  |  |
| Non-current liabilities | 1,900 | 1,865 |  |  |
| Current liabilities | 2,270 | 1,970 |  |  |
| Total equity and liabilities | 6,200 | 5,390 |  |  |

The management of Polar Finance, a large private equity investment fund, has begun a review following the sale of a substantial part of its investment portfolio. It is now considering Anchorage as a potential target for acquisition. They have contacted you and asked if you would provide a brief report on the financial performance of Anchorage Retail and give an independent view on a bid the company is considering for the business. The suggested bid would be in the form of a cash offer of $\$ 3.20$ a share which would represent a $60 \not \subset$ premium on the current share price. Reviewing the fund's existing business portfolio prior to acquisition you estimate that its asset beta is $0 \cdot 285$. Polar Finance has equity funds under management of $\$ 1,125$ million and a market based gearing ratio (debt as a proportion of total capital employed) of 0.85 . This acquisition would be financed from additional cash resources and by additional borrowing of $\$ 2.5$ billion. It is expected that Anchorage's proportion of the total post-acquisition cash flows will be $20 \%$. Polar Finance does not pay tax on its income.

During your investigations you discover the following:

1. The equity beta for Anchorage is $0 \cdot 75$. The current risk free rate is $5 \%$. In order to estimate the rate of return on the market using the dividend growth model you note that the current dividend yield on a broadly based market index is $3 \cdot 1 \%$ and the growth in GDP is $4 \%$ nominal. The growth of the firms in the index is fairly represented by growth in GDP.
2. Anchorage has a gearing ratio based upon market capitalisation of $24 \%$. You estimate that its current cost of debt capital is $6.2 \%$. You may assume that Anchorage's cost of finance has been constant over the last twelve months.

You may use year end financial position values when calculating performance ratios.

## Required:

## Prepare a report for Polar Finance:

(a) Outlining the principal risks that Polar Finance should consider when assessing an acquisition of this size.
(b) Summarising the performance of Anchorage in 2009 compared with 2008 on the basis of the EVA® for each year and using two other ratios you consider appropriate.
(c) Estimating the impact of this acquisition upon the required rate of return of equity investors in Polar Finance.
(d) Evaluating the argument that this company may have been systematically undervalued by the market and therefore a suitable target for acquisition.
(4 marks)
Professional marks will be awarded for the appropriateness of the format and presentation of the report and the effectiveness with which its advice is communicated.

## Section B - TWO questions ONLY to be attempted

3 Alaska Salvage is in discussion with potential lenders about financing an ambitious five-year project searching for lost gold in the central Atlantic. The company has had great success in the past with its various salvage operations and is now quoted on the London Alternative Investment Market. The company is currently financed by 120,000 equity shares trading at $\$ 85$ per share. It needs to borrow $\$ 1.6$ million and is concerned about the level of the fixed rates being suggested by the lenders. After lengthy discussions the lenders are prepared to offer finance against a mezzanine issue of fixed rate five-year notes with warrants attached. Each \$10,000 note, repayable at par, would carry a warrant for 100 equity shares at an exercise price of $\$ 90$ per share. The estimated volatility of the returns on the company's equity is $20 \%$ and the risk free rate of interest is $5 \%$. The company does not pay dividends to its equity investors.

You may assume that the issue of these loan notes will not influence the current value of the firm's equity. The issue will be made at par.

## Required:

(a) Estimate, using Black-Scholes Option Pricing Model as appropriate, the current value of each warrant to the lender noting the assumptions that you have made in your valuation.
(10 marks)
(b) Estimate the coupon rate that would be required by the lenders if they wanted a $13 \%$ rate of return on their investment.
(c) Discuss the advantages and disadvantages of issuing mezzanine debt in the situation outlined in the case.

4 You are the Chief Financial Officer of Moose Co. Moose Co is a manufacturer of cleaning equipment and has an international market for its products. Your company places a strong emphasis on innovation and design with patent protection across all its product range.

The company has two principal manufacturing centres, one in Europe which has been reduced in size in recent years because of high labour costs and the other in South East Asia. However, Moose Co's development has relied upon ready access to the debt market both in Europe and in South East Asia and the company is planning significant expansion with a new manufacturing and distribution centre in South America. Your company is highly profitable with strong cash flows although in the last two quarters there has been a downturn in sales in all markets as the global recession has begun to take effect.

Since August 2007, credit conditions have deteriorated across all of the major economies as banks have curtailed their lending following the down rating of US asset-backed securities. In 2008 and 2009 many banks recorded significant multibillion dollar losses as they attempted to sell off what had become known as 'toxic debt', leading to a further collapse in their value. In response many banks also attempted to repair their financial position by rights and other equity issues.

The founder and executive chairman of the company, Alan Bison, is planning a round of meetings with a number of investment banks in leading financial centres around the world to explore raising a $\$ 350$ million dollar loan for the new development. It has already been suggested that a loan of this size would need to be syndicated or alternatively raised through a bond issue.

In preparation for those meetings he has asked you to provide him with some briefing notes.

## Required:

(a) Given conditions in the global debt market as described above, advise on the likely factors banks will consider in offering a loan of this size.
(b) Assess the relative advantages of loan syndication versus a bond issue to Moose Co.
(c) Assess the relative advantages and disadvantages of entering into a capital investment of this scale at this stage of the global economic cycle.

5 To finance capital investment in its domestic market, the Katmai Company raised $\$ 150$ million through the issue of 12-year floating rate notes at 120 basis points over LIBOR, interest payable at six month intervals. Following a review of the current yield curve, the company's Chief Financial Officer has become concerned about the potential impact of rising LIBOR on the firm's future cash flows. The loan now has 10 years to maturity. The CFO asks you, his deputy, to examine the choices that are now available to the firm and to recommend the best course of action. She comments that a swap is an obvious choice but that she would appreciate a briefing on the advantages and disadvantages of the alternative approaches to managing the company's interest rate risk and an estimate of the six monthly Value at Risk (VaR) if nothing is done. As part of your investigation you note that 10-year swap rates are quoted at 5•25-5.40. In estimating the VaR you note that the firm has a policy of $95 \%$ confidence level on its exposure to non-core risk and that the annual volatility of LIBOR is currently 150 basis points.

## Required:

(a) Evaluate the alternative choices the company has for managing its interest rate exposure and recommend, with justification, the course of action the company should follow.
(9 marks)
(b) Estimate the six-monthly interest rate and the effective annual rate payable if a vanilla interest rate swap is agreed.
(c) Estimate the six monthly Value at Risk on the interest rate exposure associated with this borrowing and comment upon the interpretation of the result.
(6 marks)
(20 marks)

## Formulae

Modigliani and Miller Proposition 2 (with tax)

$$
k_{e}=k_{e}^{i}+(1-T)\left(k_{e}^{i}-k_{d}\right) \frac{V_{d}}{V_{e}}
$$

Two asset portfolio

$$
s_{p}=\sqrt{w_{a}^{2} s_{a}^{2}+w_{b}^{2} s_{b}^{2}+2 w_{a} w_{b} r_{a b} s_{a} s_{b}}
$$

The Capital Asset Pricing Model

$$
\mathrm{E}\left(\mathrm{r}_{\mathrm{i}}\right)=\mathrm{R}_{\mathrm{f}}+\beta_{\mathrm{i}}\left(\mathrm{E}\left(\mathrm{r}_{\mathrm{m}}\right)-\mathrm{R}_{\mathrm{f}}\right)
$$

The asset beta formula

$$
\beta_{\mathrm{a}}=\left[\frac{\mathrm{V}_{\mathrm{e}}}{\left(\mathrm{~V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{e}}\right]+\left[\frac{\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})}{\left(\mathrm{V}_{\mathrm{e}}+\mathrm{V}_{\mathrm{d}}(1-\mathrm{T})\right)} \beta_{\mathrm{d}}\right]
$$

## The Growth Model

$$
P_{o}=\frac{D_{0}(1+g)}{\left(r_{e}-g\right)}
$$

## Gordon's growth approximation

$$
\mathrm{g}=\mathrm{br} \mathrm{r}_{\mathrm{e}}
$$

The weighted average cost of capital

$$
\text { WACC }=\left[\frac{V_{e}}{V_{e}+V_{d}}\right] k_{e}+\left[\frac{V_{d}}{V_{e}+V_{d}}\right] k_{d}(1-T)
$$

## The Fisher formula

$$
(1+i)=(1+r)(1+h)
$$

Purchasing power parity and interest rate parity

$$
S_{1}=S_{0} \times \frac{\left(1+h_{c}\right)}{\left(1+h_{b}\right)} \quad F_{0}=S_{0} \times \frac{\left(1+i_{c}\right)}{\left(1+i_{b}\right)}
$$

## The Put Call Parity relationship

$$
\mathrm{p}=\mathrm{c}-\mathrm{P}_{\mathrm{a}}+\mathrm{P}_{\mathrm{e}} \mathrm{e}^{-\mathrm{rt}}
$$

Modified Internal Rate of Return

$$
M I R R=\left[\frac{P V_{R}}{P V_{l}}\right]^{\frac{1}{n}}\left(1+r_{e}\right)-1
$$



## Present Value Table

Present value of 1 i.e. $(1+r)^{-n}$
$\begin{array}{ll}\text { Where } & r=\text { discount rate } \\ & n=\text { number of periods until payment }\end{array}$

Discount rate (r)
Periods

| (n) | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 | 2 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 | 3 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 | 4 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0.705 | 0.666 | 0.630 | 0.596 | 0.564 | 6 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 | 7 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 | 8 |
| 9 | 0.941 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 | 9 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.305 | 11 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 | 12 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 | 13 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 | 14 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 | 15 |


| $(\mathrm{n})$ | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 | 2 |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 | 3 |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 | 4 |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 | 5 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 | 6 |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 | 7 |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 | 8 |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 | 9 |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 | 10 |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 | 11 |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 | 12 |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 | 13 |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 | 14 |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.074 | 0.065 | 15 |

## Annuity Table

Present value of an annuity of 1 i.e. $\frac{1-(1+r)^{-n}}{r}$

$$
\begin{array}{ll}
\text { Where } & r=\text { discount rate } \\
& n=\text { number of periods }
\end{array}
$$

## Discount rate (r)

Periods

| ( n ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 | 1 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 | 2 |
| 3 | 2.941 | $2 \cdot 884$ | 2.829 | $2 \cdot 775$ | $2 \cdot 723$ | $2 \cdot 673$ | $2 \cdot 624$ | 2.577 | $2 \cdot 531$ | 2.487 | 3 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | $3 \cdot 465$ | $3 \cdot 387$ | 3.312 | 3.240 | $3 \cdot 170$ | 4 |
| 5 | 4.853 | $4 \cdot 713$ | 4.580 | $4 \cdot 452$ | $4 \cdot 329$ | $4 \cdot 212$ | 4.100 | 3.993 | 3.890 | $3 \cdot 791$ | 5 |
| 6 | 5.795 | 5.601 | $5 \cdot 417$ | $5 \cdot 242$ | 5.076 | 4.917 | $4 \cdot 767$ | $4 \cdot 623$ | $4 \cdot 486$ | 4.355 | 6 |
| 7 | $6 \cdot 728$ | 6.472 | 6.230 | 6.002 | $5 \cdot 786$ | $5 \cdot 582$ | $5 \cdot 389$ | $5 \cdot 206$ | 5.033 | 4.868 | 7 |
| 8 | $7 \cdot 652$ | 7.325 | 7.020 | $6 \cdot 733$ | $6 \cdot 463$ | $6 \cdot 210$ | 5.971 | $5 \cdot 747$ | $5 \cdot 535$ | $5 \cdot 335$ | 8 |
| 9 | $8 \cdot 566$ | $8 \cdot 162$ | 7.786 | 7.435 | $7 \cdot 108$ | 6.802 | 6.515 | $6 \cdot 247$ | 5.995 | 5.759 | 9 |
| 10 | $9 \cdot 471$ | 8.983 | 8.530 | $8 \cdot 111$ | $7 \cdot 722$ | $7 \cdot 360$ | $7 \cdot 024$ | $6 \cdot 710$ | 6.418 | $6 \cdot 145$ | 10 |
| 11 | $10 \cdot 37$ | 9.787 | 9.253 | 8.760 | $8 \cdot 306$ | 7.887 | $7 \cdot 499$ | $7 \cdot 139$ | 6.805 | 6.495 | 11 |
| 12 | $11 \cdot 26$ | $10 \cdot 58$ | 9.954 | $9 \cdot 385$ | 8.863 | 8.384 | 7.943 | 7.536 | $7 \cdot 161$ | 6.814 | 12 |
| 13 | $12 \cdot 13$ | 11.35 | $10 \cdot 63$ | 9.986 | $9 \cdot 394$ | 8.853 | 8.358 | 7.904 | 7.487 | $7 \cdot 103$ | 13 |
| 14 | 13.00 | $12 \cdot 11$ | 11.30 | $10 \cdot 56$ | 9.899 | $9 \cdot 295$ | $8 \cdot 745$ | 8.244 | 7.786 | $7 \cdot 367$ | 14 |
| 15 | 13.87 | $12 \cdot 85$ | 11.94 | $11 \cdot 12$ | $10 \cdot 38$ | $9 \cdot 712$ | $9 \cdot 108$ | 8.559 | 8.061 | $7 \cdot 606$ | 15 |
| ( n ) | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | $0 \cdot 870$ | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 | 1 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 | 2 |
| 3 | $2 \cdot 444$ | 2.402 | $2 \cdot 361$ | $2 \cdot 322$ | $2 \cdot 283$ | $2 \cdot 246$ | $2 \cdot 210$ | $2 \cdot 174$ | $2 \cdot 140$ | $2 \cdot 106$ | 3 |
| 4 | $3 \cdot 102$ | 3.037 | 2.974 | 2.914 | $2 \cdot 855$ | $2 \cdot 798$ | $2 \cdot 743$ | $2 \cdot 690$ | 2.639 | 2.589 | 4 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | $3 \cdot 199$ | $3 \cdot 127$ | 3.058 | 2.991 | 5 |
| 6 | $4 \cdot 231$ | $4 \cdot 111$ | 3.998 | 3.889 | $3 \cdot 784$ | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 | 6 |
| 7 | $4 \cdot 712$ | 4.564 | 4.423 | $4 \cdot 288$ | $4 \cdot 160$ | 4.039 | $3 \cdot 922$ | 3.812 | 3.706 | $3 \cdot 605$ | 7 |
| 8 | $5 \cdot 146$ | 4.968 | $4 \cdot 799$ | 4.639 | 4.487 | 4.344 | $4 \cdot 207$ | 4.078 | 3.954 | 3.837 | 8 |
| 9 | $5 \cdot 537$ | $5 \cdot 328$ | $5 \cdot 132$ | 4.946 | $4 \cdot 772$ | $4 \cdot 607$ | $4 \cdot 451$ | 4.303 | 4.163 | 4.031 | 9 |
| 10 | $5 \cdot 889$ | $5 \cdot 650$ | $5 \cdot 426$ | $5 \cdot 216$ | 5.019 | $4 \cdot 833$ | $4 \cdot 659$ | $4 \cdot 494$ | $4 \cdot 339$ | 4.192 | 10 |
| 11 | 6.207 | 5.938 | 5.687 | 5.453 | $5 \cdot 234$ | 5.029 | 4.836 | 4.656 | $4 \cdot 486$ | 4.327 | 11 |
| 12 | $6 \cdot 492$ | 6.194 | 5.918 | $5 \cdot 660$ | $5 \cdot 421$ | $5 \cdot 197$ | 4.988 | 4.793 | $4 \cdot 611$ | 4.439 | 12 |
| 13 | $6 \cdot 750$ | $6 \cdot 424$ | $6 \cdot 122$ | $5 \cdot 842$ | 5.583 | $5 \cdot 342$ | $5 \cdot 118$ | 4.910 | $4 \cdot 715$ | 4.533 | 13 |
| 14 | 6.982 | 6.628 | $6 \cdot 302$ | 6.002 | $5 \cdot 724$ | $5 \cdot 468$ | $5 \cdot 229$ | 5.008 | 4.802 | 4.611 | 14 |
| 15 | $7 \cdot 191$ | $6 \cdot 811$ | $6 \cdot 462$ | $6 \cdot 142$ | $5 \cdot 847$ | $5 \cdot 575$ | $5 \cdot 324$ | 5.092 | $4 \cdot 876$ | $4 \cdot 675$ | 15 |

Standard normal distribution table

|  | $0 \cdot 00$ | 0.01 | $0 \cdot 02$ | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0 \cdot 0$ | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| $0 \cdot 1$ | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| $0 \cdot 2$ | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | $0 \cdot 1026$ | $0 \cdot 1064$ | $0 \cdot 1103$ | 0.1141 |
| $0 \cdot 3$ | 0.1179 | 0.1217 | $0 \cdot 1255$ | $0 \cdot 1293$ | $0 \cdot 1331$ | $0 \cdot 1368$ | $0 \cdot 1406$ | 0.1443 | $0 \cdot 1480$ | $0 \cdot 1517$ |
| $0 \cdot 4$ | $0 \cdot 1554$ | $0 \cdot 1591$ | $0 \cdot 1628$ | $0 \cdot 1664$ | $0 \cdot 1700$ | $0 \cdot 1736$ | $0 \cdot 1772$ | $0 \cdot 1808$ | $0 \cdot 1844$ | $0 \cdot 1879$ |
| 0.5 | $0 \cdot 1915$ | $0 \cdot 1950$ | $0 \cdot 1985$ | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| $0 \cdot 6$ | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.2580 | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | $0 \cdot 2881$ | 0.2910 | 0.2939 | 0.2967 | 0.2995 | $0 \cdot 3023$ | 0.3051 | $0 \cdot 3078$ | 0.3106 | 0.3133 |
| 0.9 | $0 \cdot 3159$ | 0.3186 | 0.3212 | 0.3238 | 0.3264 | $0 \cdot 3289$ | 0.3315 | $0 \cdot 3340$ | $0 \cdot 3365$ | 0.3389 |
| 1.0 | $0 \cdot 3413$ | $0 \cdot 3438$ | 0.3461 | $0 \cdot 3485$ | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| $1 \cdot 1$ | $0 \cdot 3643$ | $0 \cdot 3665$ | 0.3686 | $0 \cdot 3708$ | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| $1 \cdot 2$ | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | $0 \cdot 4222$ | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| $2 \cdot 1$ | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| $2 \cdot 2$ | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| $2 \cdot 3$ | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| $2 \cdot 4$ | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| $2 \cdot 6$ | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| $2 \cdot 7$ | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| $2 \cdot 8$ | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| $2 \cdot 9$ | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.0 | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.4990 | 0.4990 |

This table can be used to calculate $N(d)$, the cumulative normal distribution functions needed for the Black-Scholes model of option pricing. If $d_{i}>0$, add 0.5 to the relevant number above. If $d_{i}<0$, subtract the relevant number above from 0.5 .

## End of Question Paper

